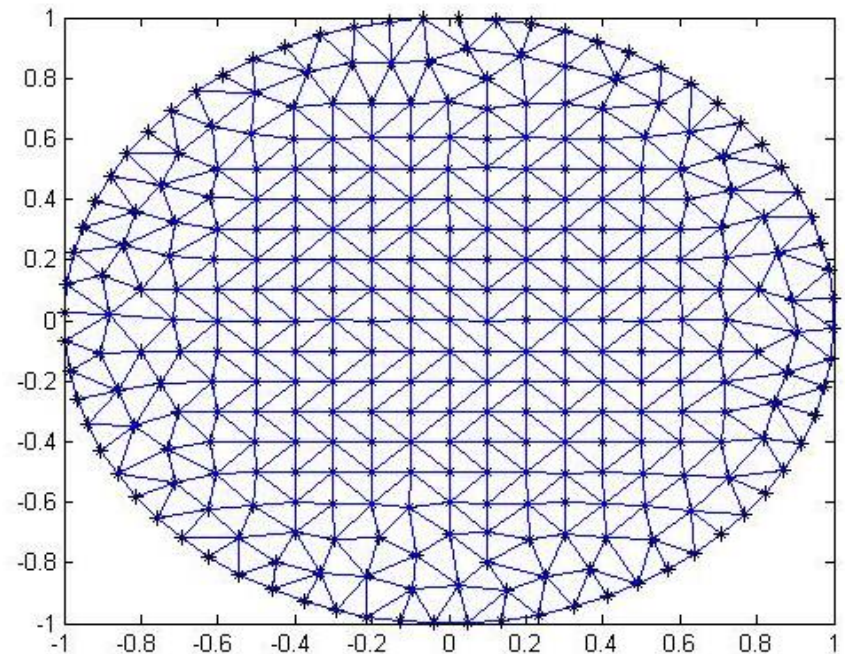


Triangle Mesh Optimization

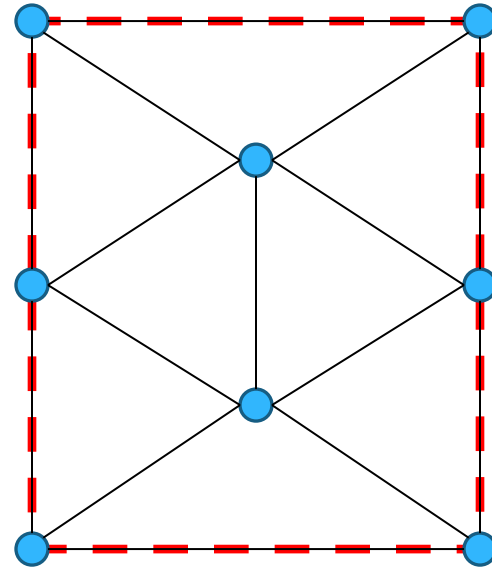
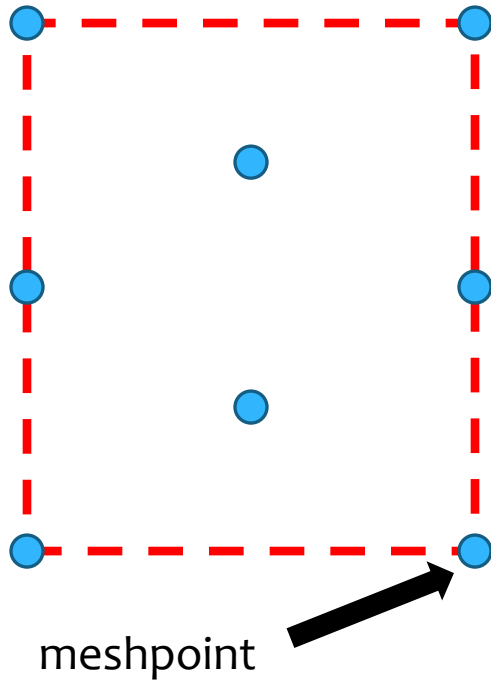
By: Jonathan Heath
Mentor: Shawn Walker

Outline

- * Background
- * Distributing Meshpoints
- * Projection Method
- * k Nearest Neighbors
- * Exterior Domain
- * Outer Boundary Force
- * Results
- * Conclusion



Background

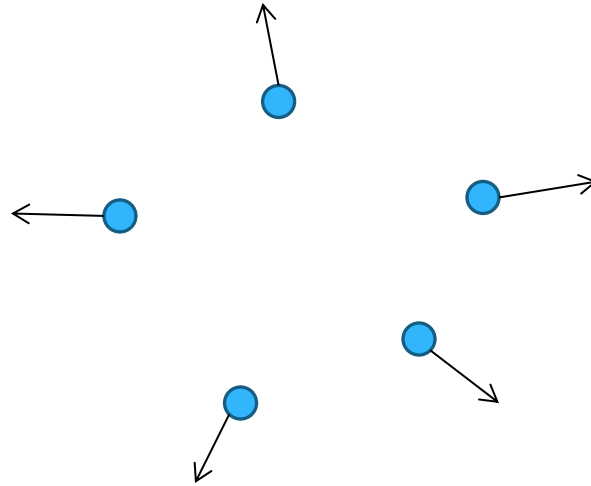


Meshes are commonly used in computer graphics and simulations.

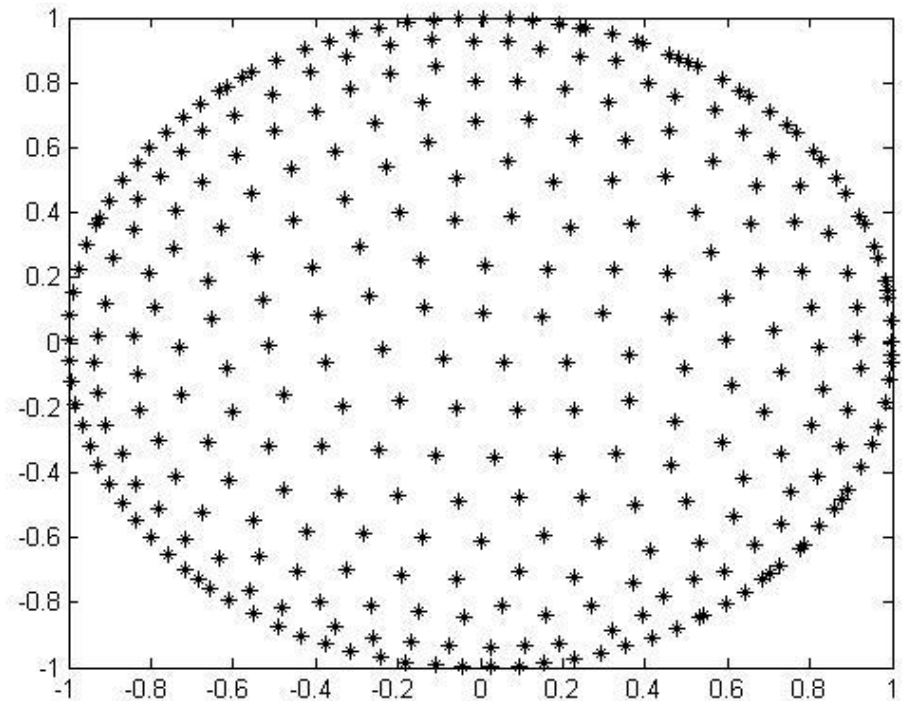
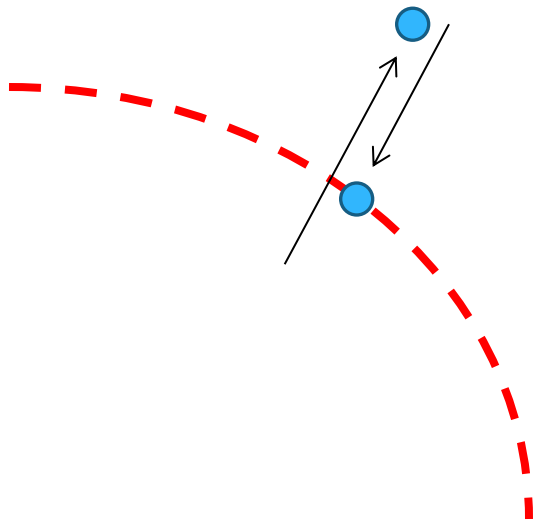
Distributing Meshpoints

Coulomb's Law:

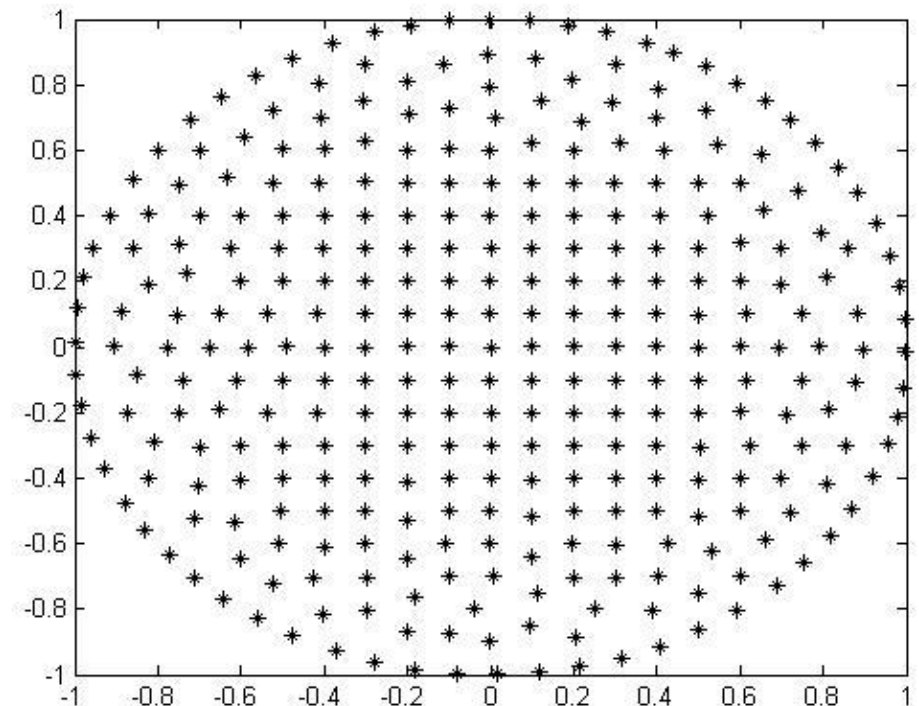
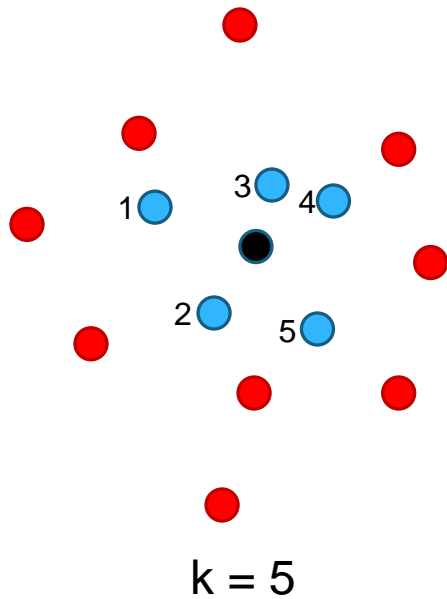
$$F(r) = k_e q \sum_{i=1}^N q_i \frac{r - r_i}{|r - r_i|^3}$$



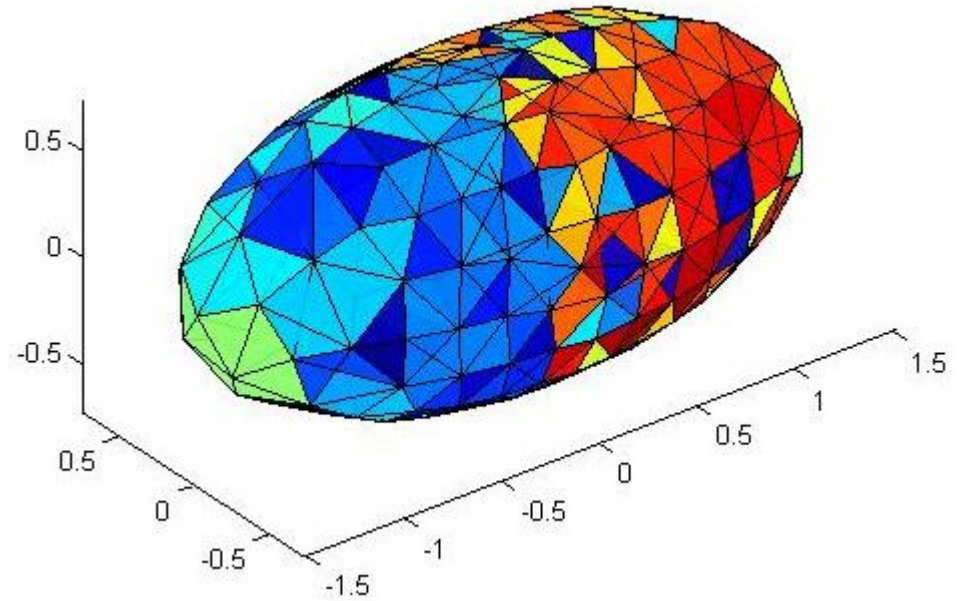
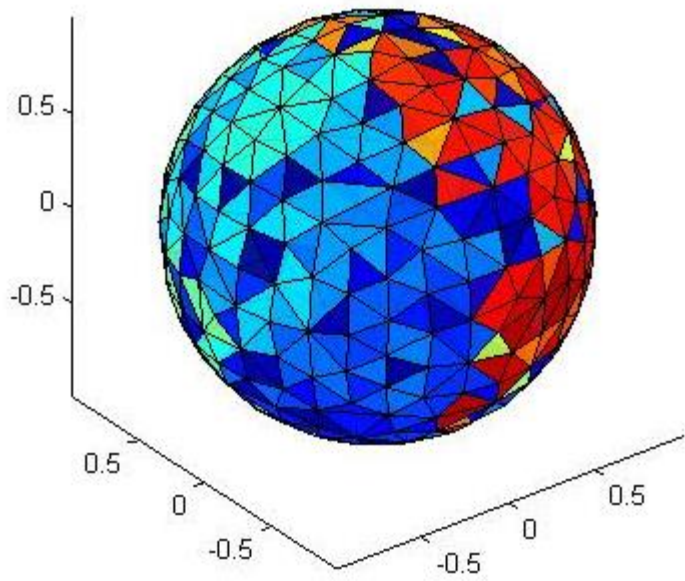
Projection Method



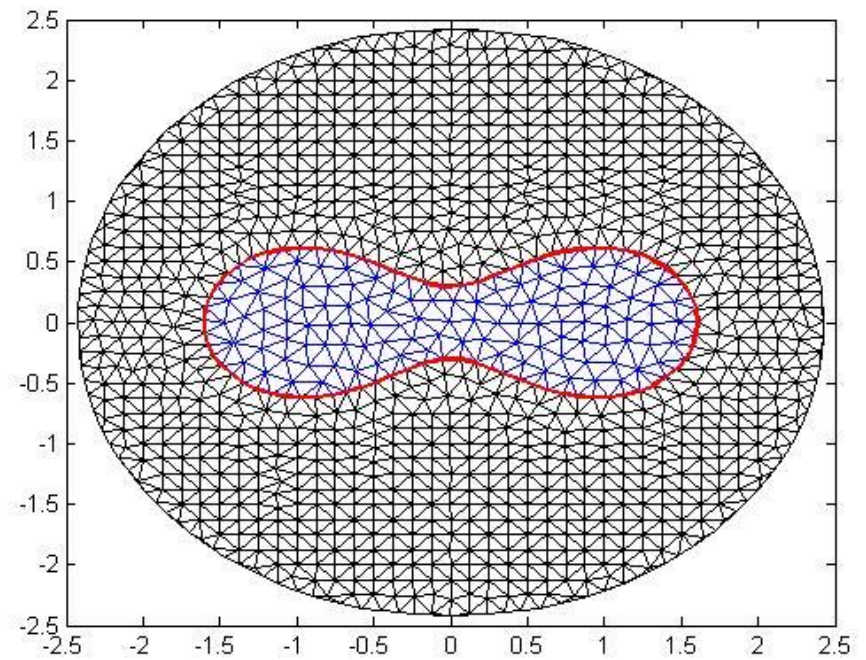
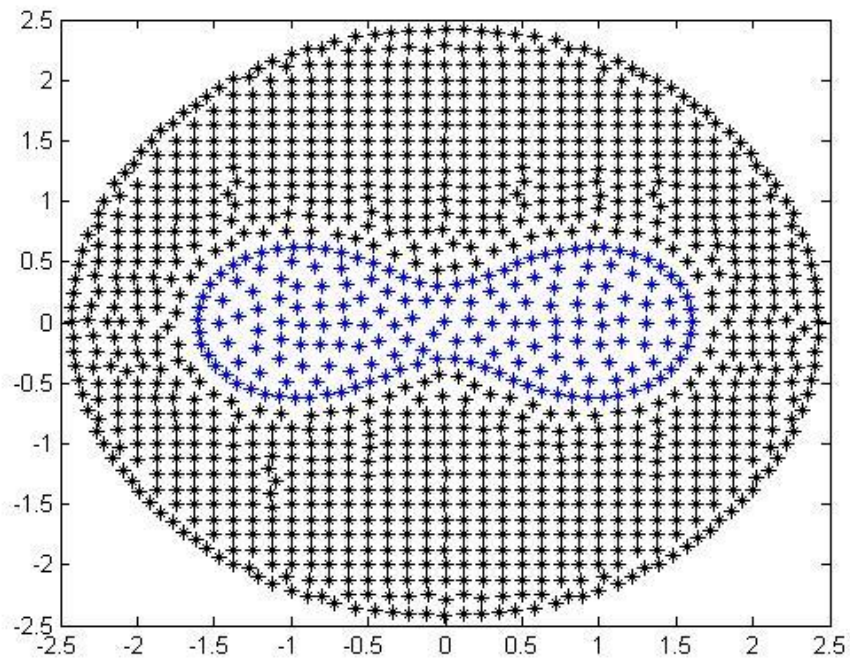
k Nearest Neighbors



3-D Case

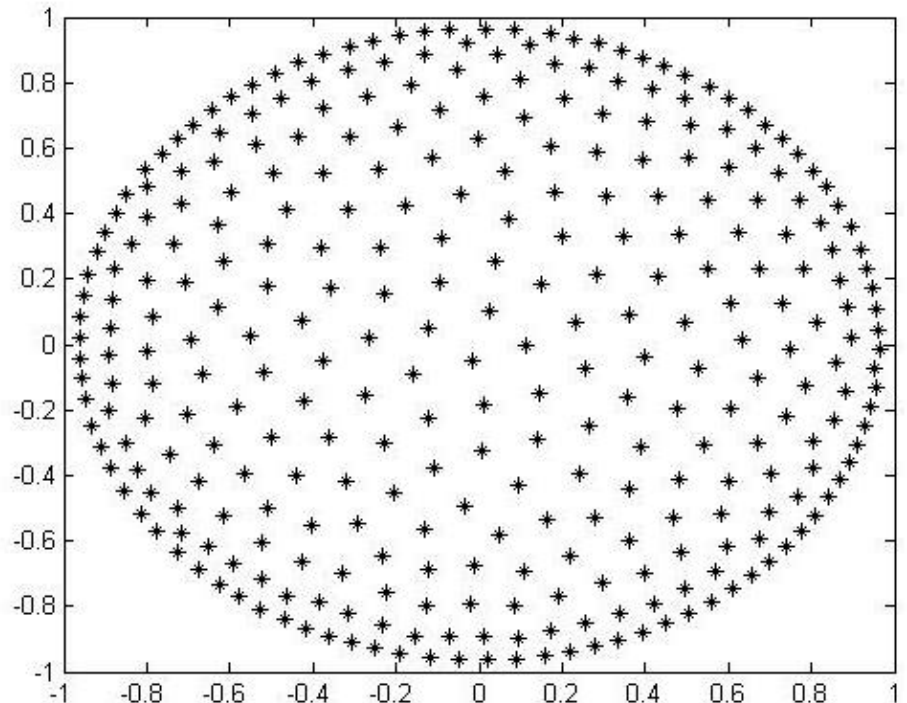
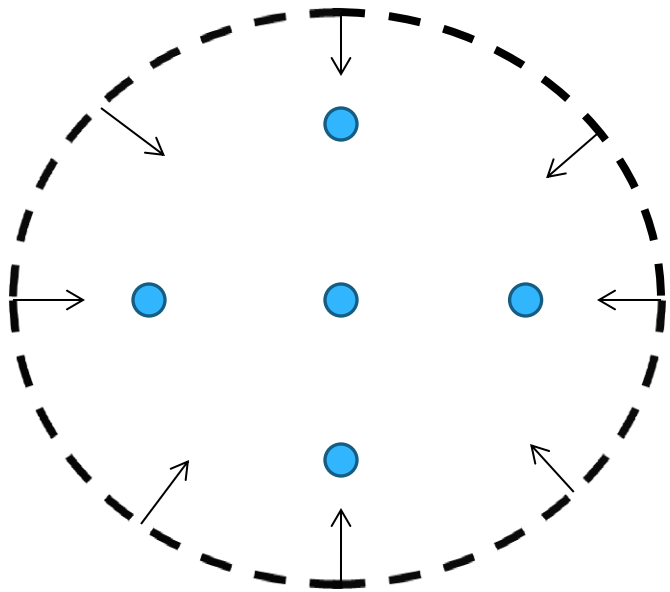


Exterior Domain



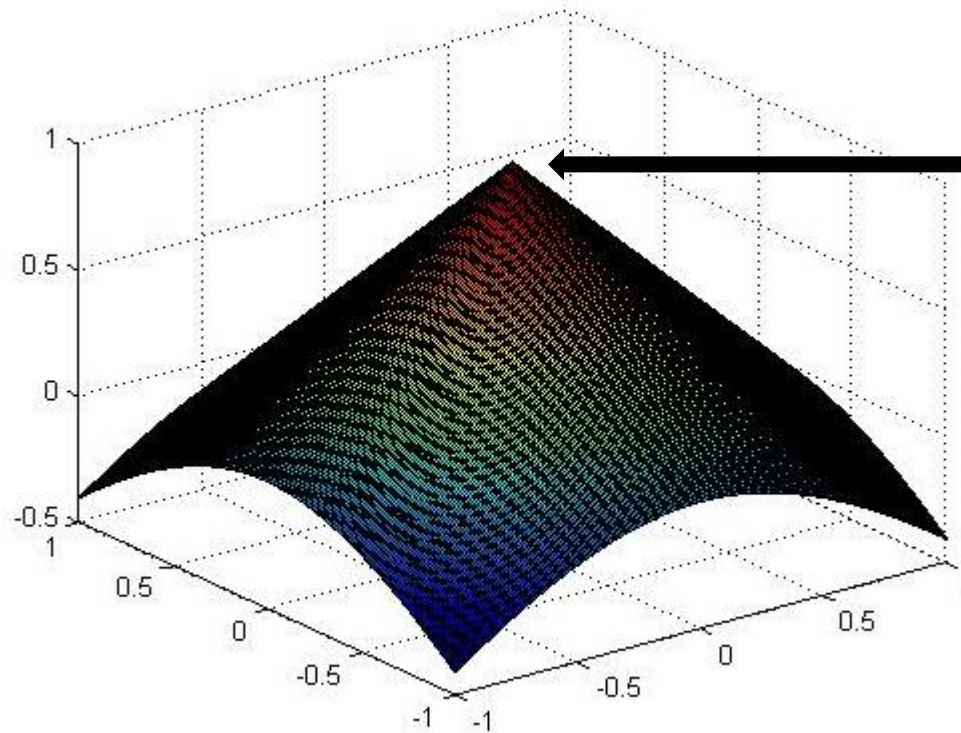
Outer Boundary Force

$$F_b(\phi) = k_e q^2 \frac{\nabla\phi(\phi + 1)}{\phi^2} e^{-\phi}$$



Signed Distance Function

circle: $\phi = C - \sqrt{x^2 + y^2}$

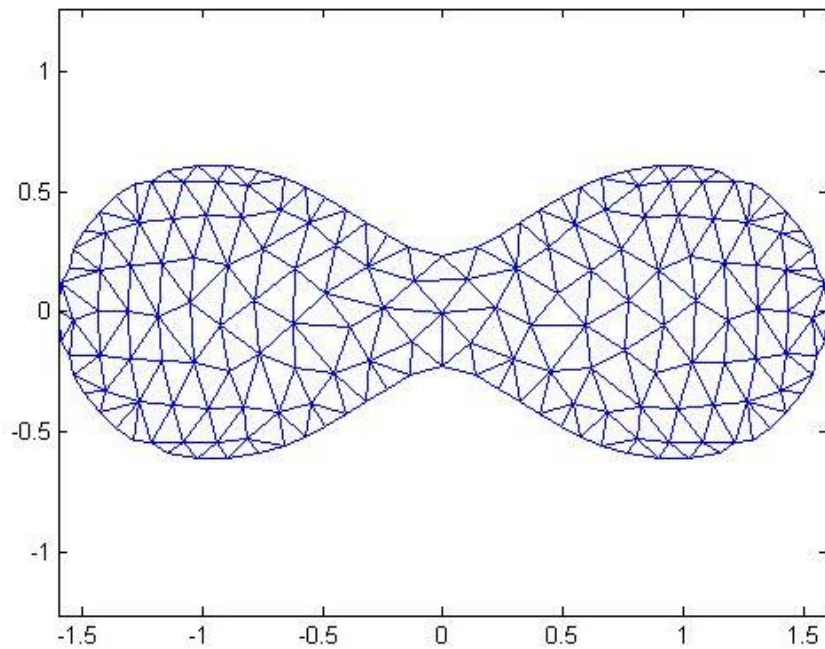


center of
circle

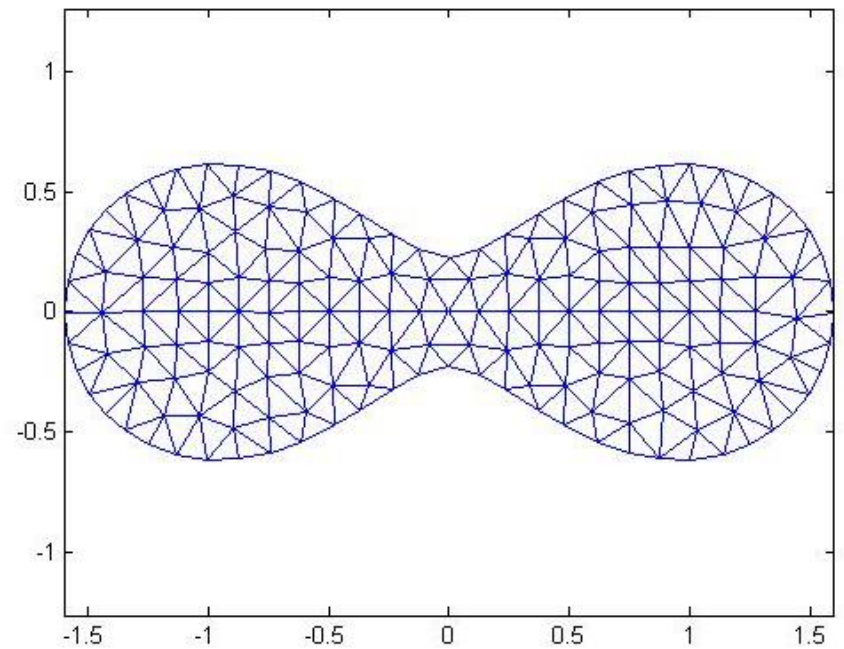
$C = 1$

Comparison

All Points

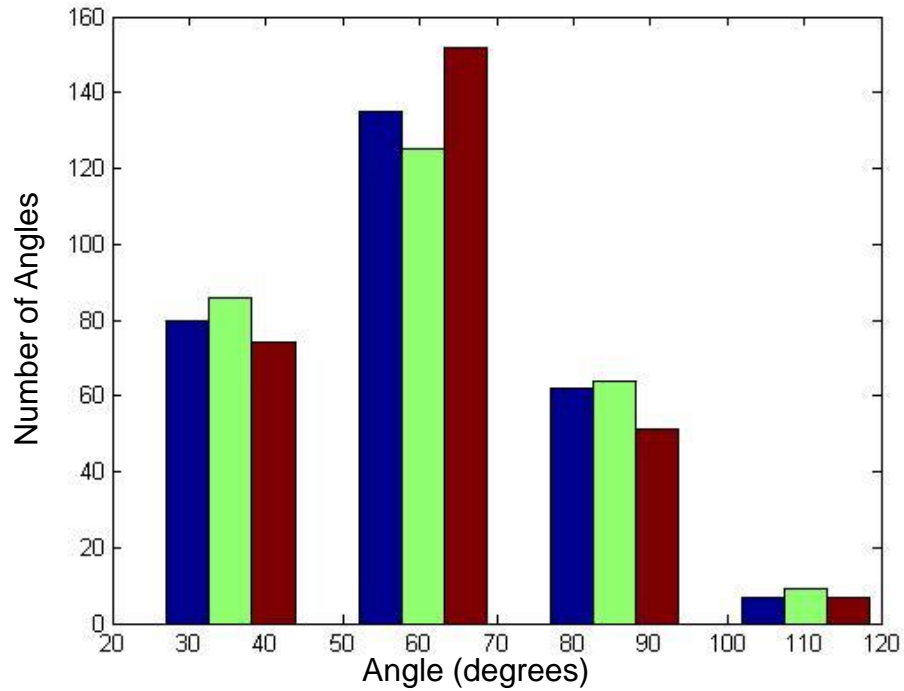


15 Nearest Neighbors

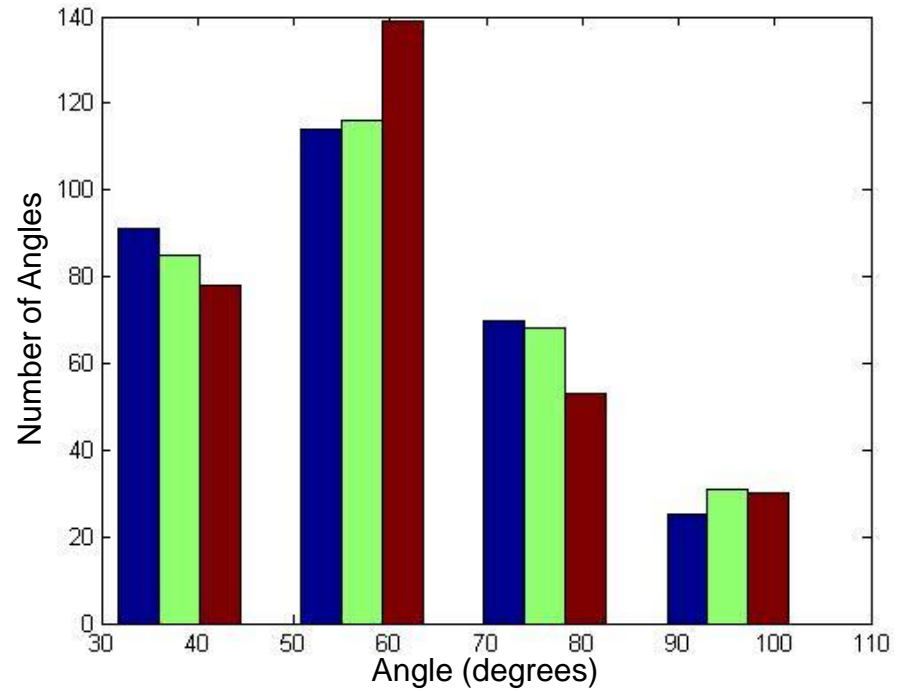


Comparison

All Points



15 Nearest Neighbors



Conclusion

- * Meshpoints were distributed across a given domain by giving the points properties that of electric charges.
- * Mesh quality was improved through the projection and k nearest neighbors methods.
- * Future work includes decreasing computation time (ex: writing C code) and exploring further into using a second domain to improve mesh quality.

Questions?

